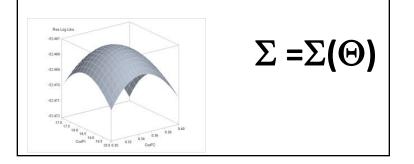
# Introduction to Likelihood Methods for SEM

#### Jarrett E. K. Byrnes University of Massachusetts Boston



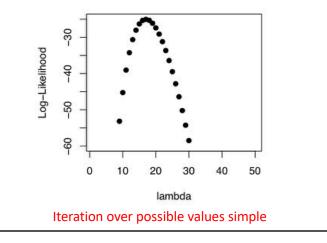
# What is Covariance-Based SEM Estimation with Likelihood?

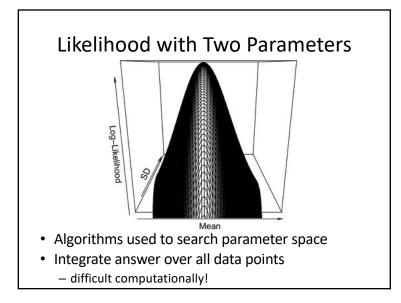
- Estimation of parameters given covariance of the data
- Equivalent to Linear Regressions, but...
- Estimation of each parameter influences the others
- Can accomodate unobserved (latent) variables and feedbacks

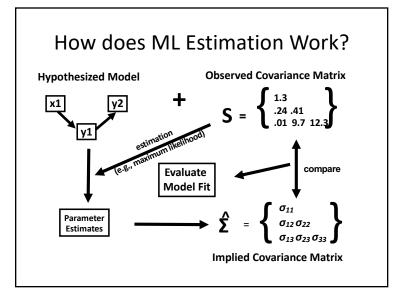
### A Likely Outline

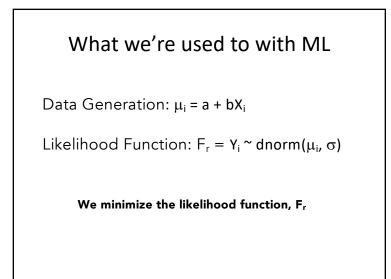
- 1. What SEM using likelihood and covariance matrices?
- 2. Model Identifiability
- 3. Sample Size for SEM
- 4. Introduction to lavaan

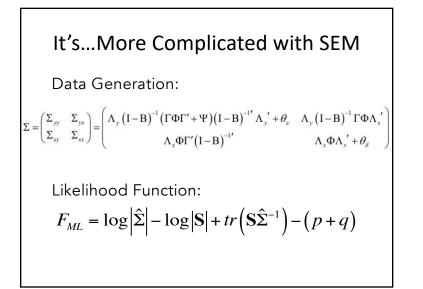
### Maximizing Likelihood with One Parameter

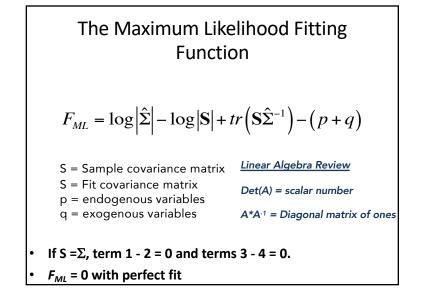


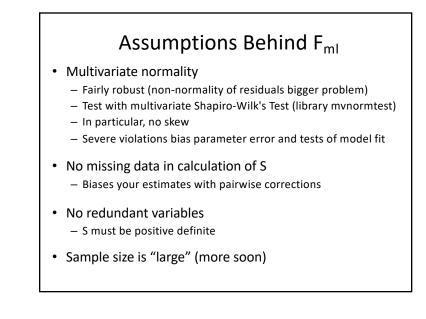












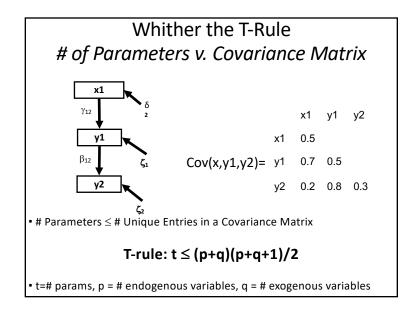
### A Likely Outline

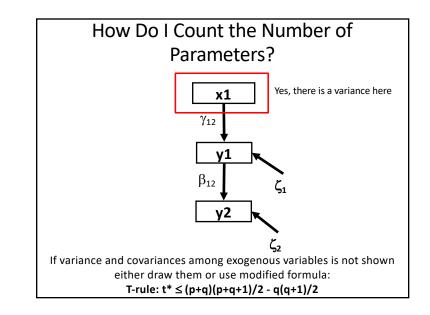
- 1. What is different about fitting using likelihood and covariance matrices?
- 2. Identifiability
- 3. Sample Size (for likelihood and piecewise approaches)
- 4. Introduction to lavaan

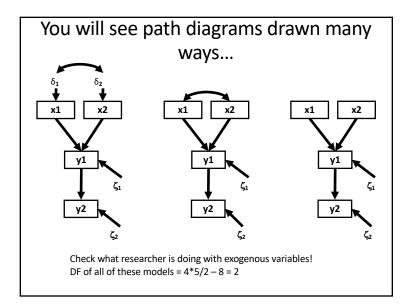
### Identifiability

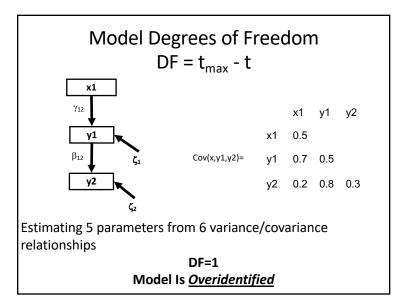
- 1. To fit a model, it must be identified
- 2. We need as much unique information as parameters
- 3. What can make a model non-identified?
  - Too many paths relative to # of variables
  - Certain model structures
  - High multicollinearity (r>0.9)
  - Complex model & small sample

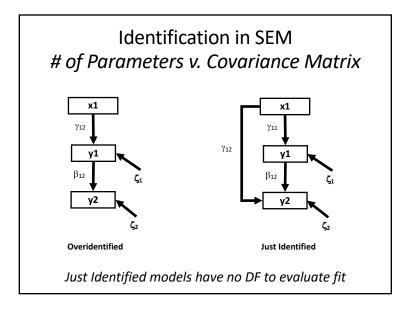
4. How do I know if my model is identified?

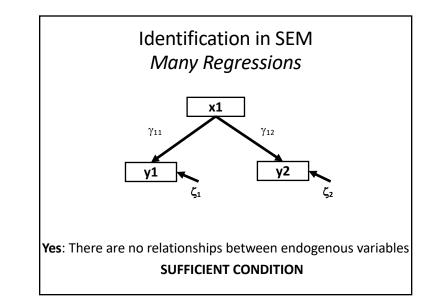


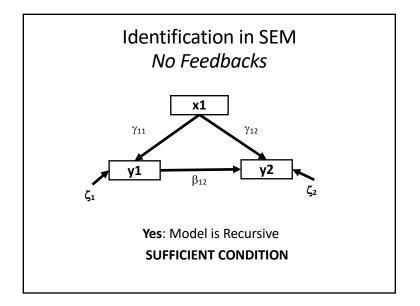


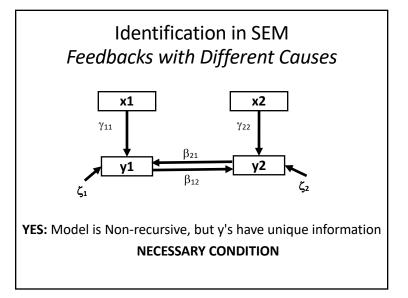


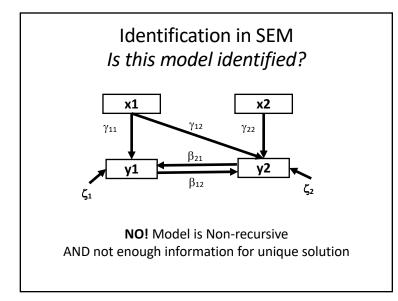


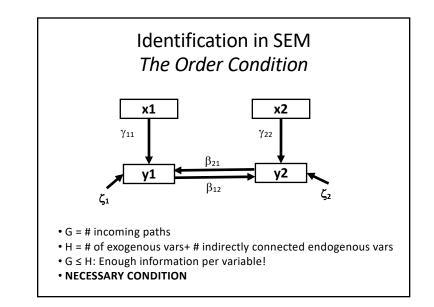


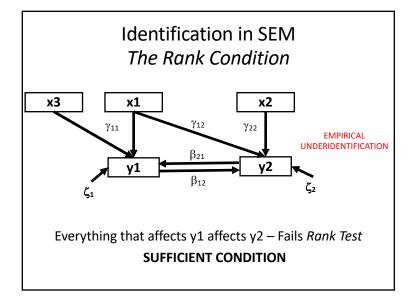












### **Rules of Identification**

#### **Necessary**

- Fewer parameters than entries in covariance diagonal matrix (T-Rule)
- Fewer incoming paths than # of variables connected to (Order condition for non-recursive models)

#### **Sufficient**

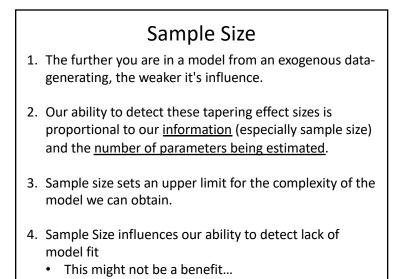
- No paths between endogenous variables
- Model is recursive
- Unique effects on endogenous variables in a feedback (Rank Condition)

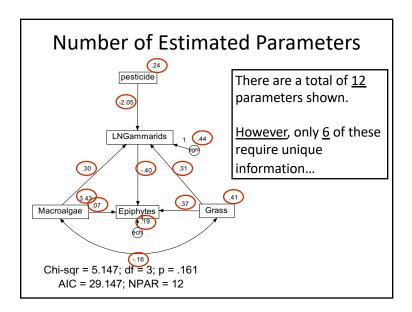
## A Likely Outline

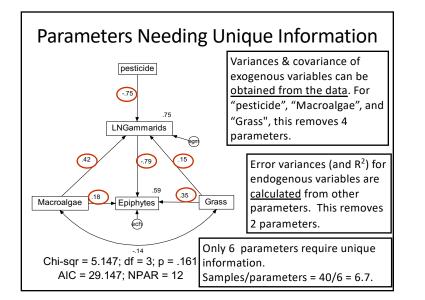
- 1. What is different about fitting using likelihood and covariance matrices?
- 2. Identifiability
- 3. Sample Size
- 4. Introduction to lavaan

# So...What's my Sample Size?

- 1. <u>Rules of thumb for sample size</u> at least 5 samples per estimated parameter
  - prefer 20 samples per parameter
  - Really, p<sup>3/2</sup>/n should approach 0 (Portnoy 1988)
- 2. Path coefficients add to our parameter list, not the variances







# A Likely Outline

- 1. What is different about fitting using likelihood and covariance matrices?
- 2. Identifiability
- 3. Sample Size (for likelihood and piecewise approaches)
- 4. Introduction to lavaan

### What is lavaan?

- Stands for LAtent VAriable Analaysis
- Written by Yves Roseel in 2010
- Currently in version 5, but 6 coming soon
- Uses R lm syntax

### A Reminder

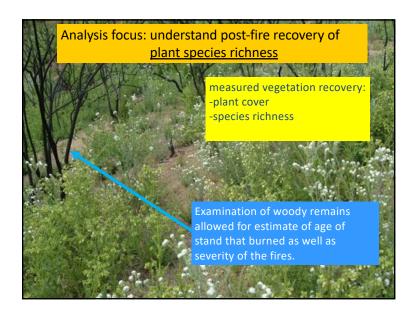
1. SOFTWARE IS A TOOL

2. IT IS NOT PERFECT

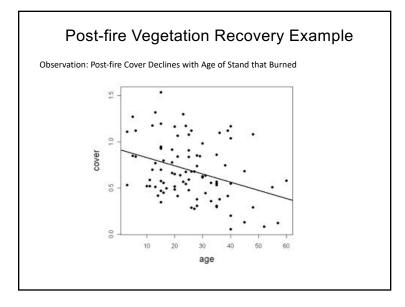
3. ALWAYS MAKE SURE IT IS DOING WHAT YOU THINK IT IS DOING! Mediation in Analysis of Post-Fire Recovery of Plant Communities in California Shrublands\*

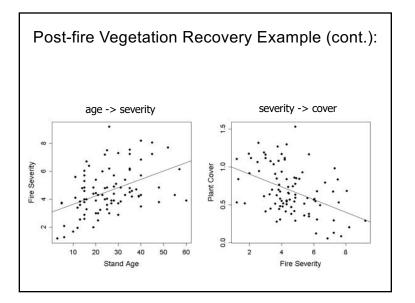


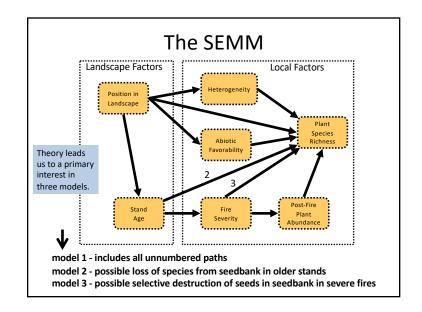
(20 x 50m), (data from Jon Keeley et al.)

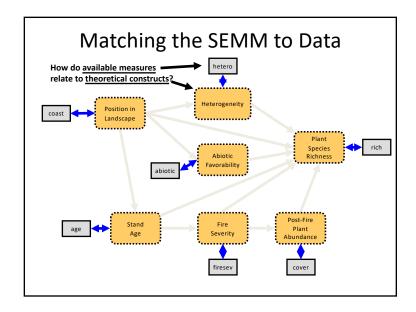


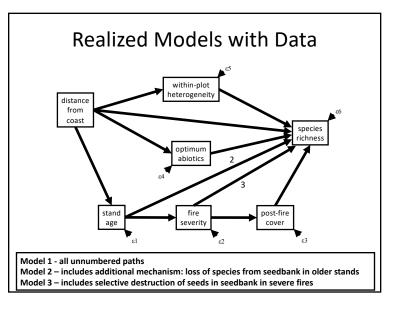


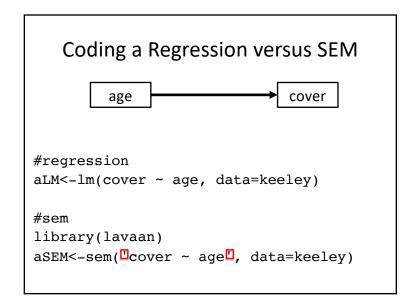








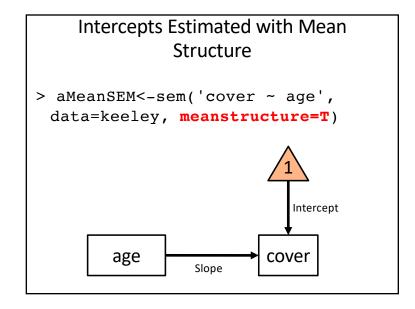


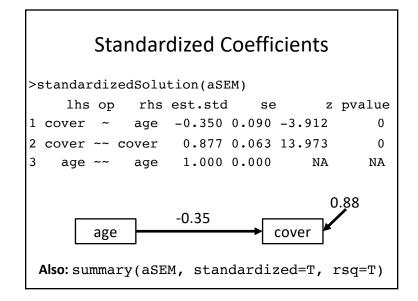


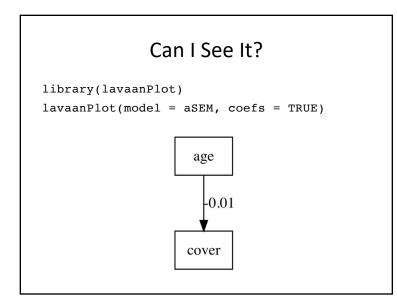
summary(aSEM)									
lavaan (0.5-23.1097) converged normally after 10 iterations									
Number of observations Estimator Minimum Function Test Statistic Degrees of freedom 90 ML 0.000 0									
Parameter estimat	es:								
Information Standard Errors				Expected Standard					
Regressions: cover ~				P(> z )					
age				0.000					

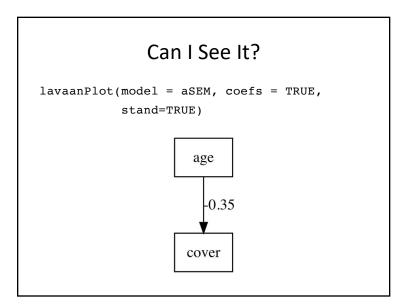
Compare to Regression							
Estimate Std.err Z-value P(> z ) Regressions: cover ~ age -0.009 0.002 -3.549 0.000							
Variances: .cover 0.087 0.013 > summary(aLM)							
Coefficients: Estimate Std. Error t value Pr(> t ) (Intercept) 0.917395 0.071726 12.79 < 2e-16 *** age -0.008846 0.002520 -3.51 0.00071 ***  Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1							
Residual standard error: 0.2988 on 88 degrees of freedom But what about the intercept?							

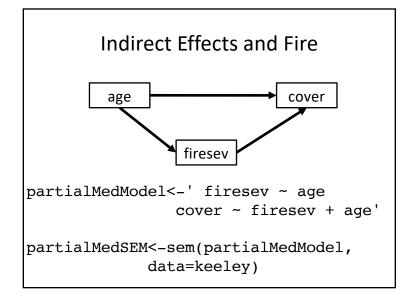
Intercepts Estimated with Mean Structure								
<pre>&gt; aMeanSEM&lt;-sem('cover ~ age', data=keeley, meanstructure=T)</pre>								
<pre>&gt; summary(aMeanSEM)</pre>								
 Regressions:	Estimate	Std.err	Z-value	P(> z )				
cover ~ age	-0.009	0.002	-3.549	0.000				
Intercepts: .cover	0.917	0.071	12.935	0.000				
Variances: .cover	0.087	0.013						

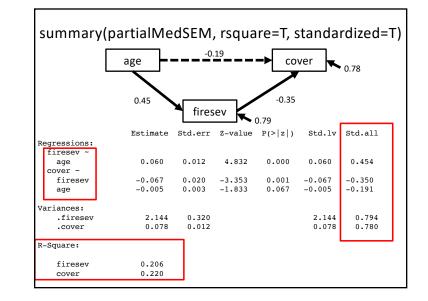


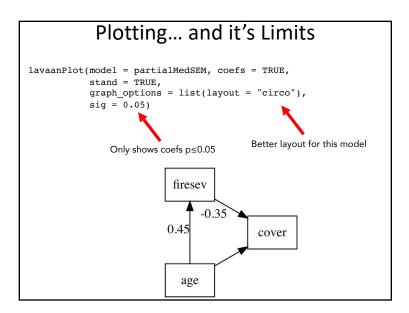


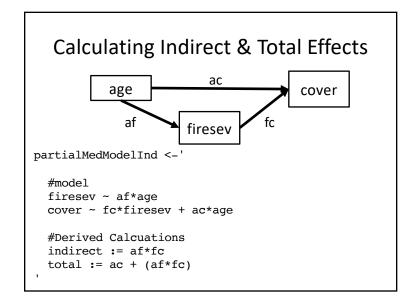


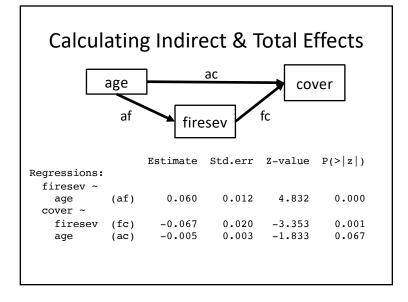


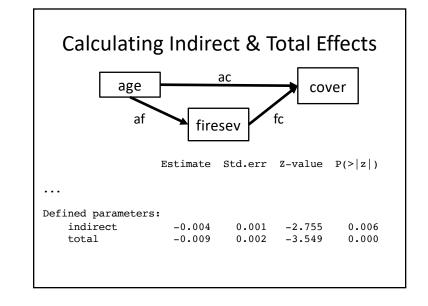


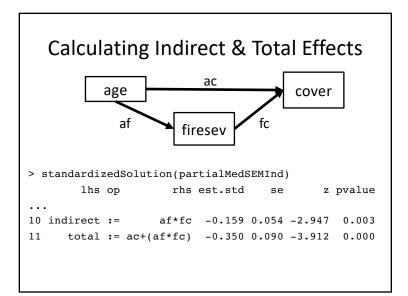


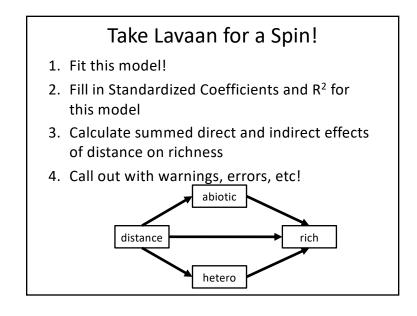




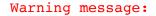












```
In lav_data_full(data = data, group =
group, cluster = cluster, :
    lavaan WARNING: some observed
variances are (at least) a factor
1000 times larger than others; use
varTable(fit) to investigate
```

### **Diagnosing Error Issues**

- 1. Does it indicate an outlier or data problem?
- 2. This is a likelihood algorithm problem can be fine!
- 3. If you are worried, rescale by 10s, see if answers change

